

EFFECTS OF SURFACE CHARGE DENSITY AND DISTRIBUTION ON THE NANOCCHANNEL ELECTRO-OSMOTIC FLOW

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Paul F. Mlakar, John F. Peters

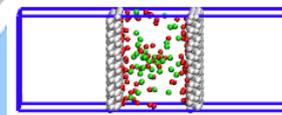
Senior Research Scientists

GSL, U.S. Army ERDC Vicksburg, MS



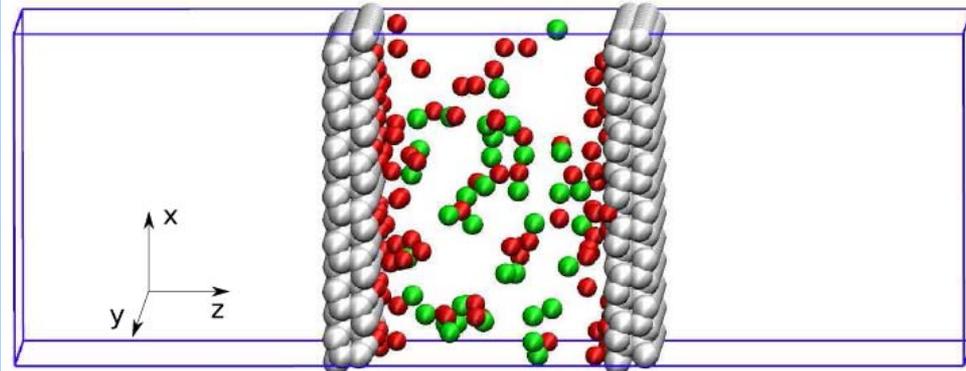
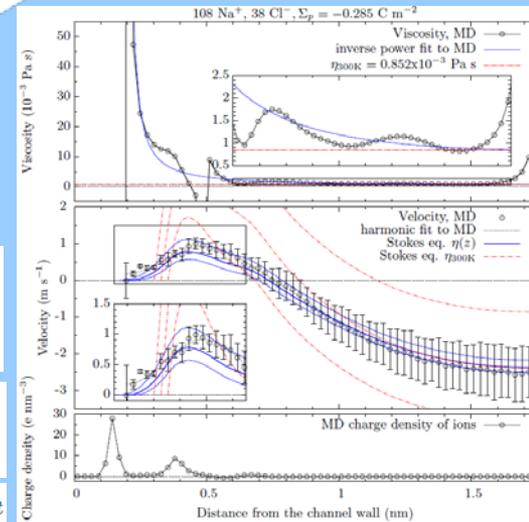
MISSISSIPPI STATE
UNIVERSITY
CAVS

US Army Corps of Engineers
BUILDING STRONG



$$\frac{d}{dz} \left[\eta(z) \frac{du_x(z)}{dz} \right] = -F_d(z)$$

$$F_d(z) = e [c_{Na^+}(z) - c_{Cl^-}(z)] E_{ext}$$



Other project

Development of MEAM potential for Al-Si-Mg-Cu-Fe alloys

B. Jelinek, S. Groh, A. Moitra, M. Horstemeyer, J. Houze,
S-G. Kim, G. Wagner, M. Baskes

<http://arxiv.org/abs/1107.0544>

Scripts to reproduce some of the potential tests

<http://code.google.com/p/ase-atomistic-potential-tests>

using Atomistic Simulation Environment (ASE)

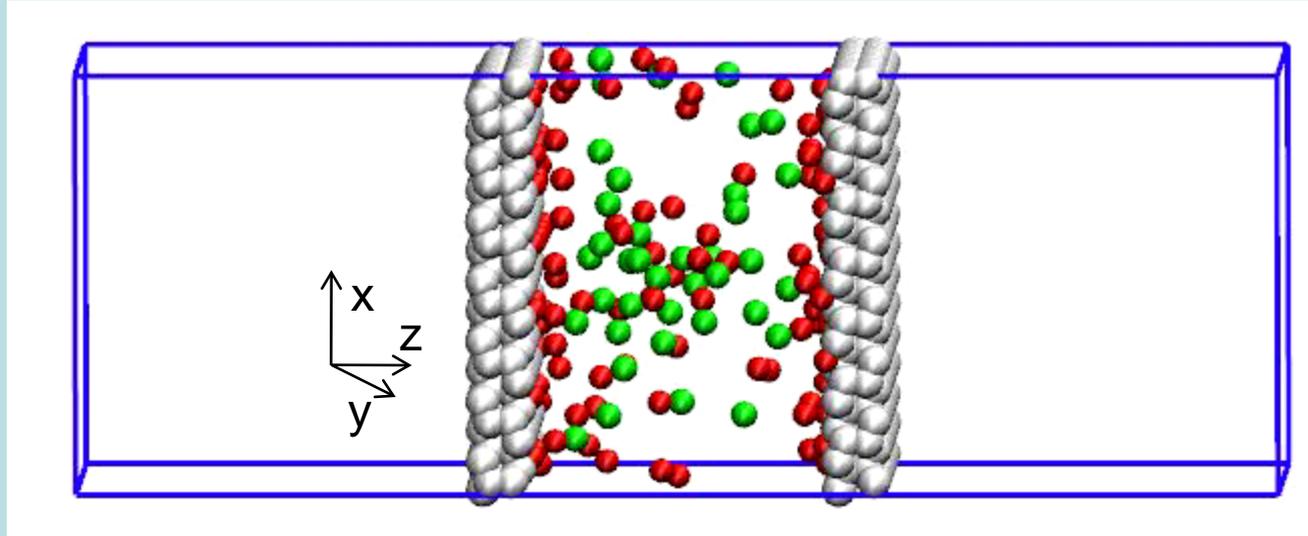
<https://wiki.fysik.dtu.dk/ase>

motivation for using ASE - talk at the NIST 2011 workshop

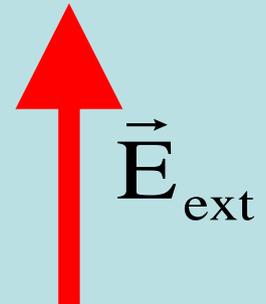
<http://www.ctcms.nist.gov/potentials/activities.html>

CAVS cyberinfrastructure site <https://ccg.hpc.msstate.edu>

Electro-osmotic flow model



Electric field



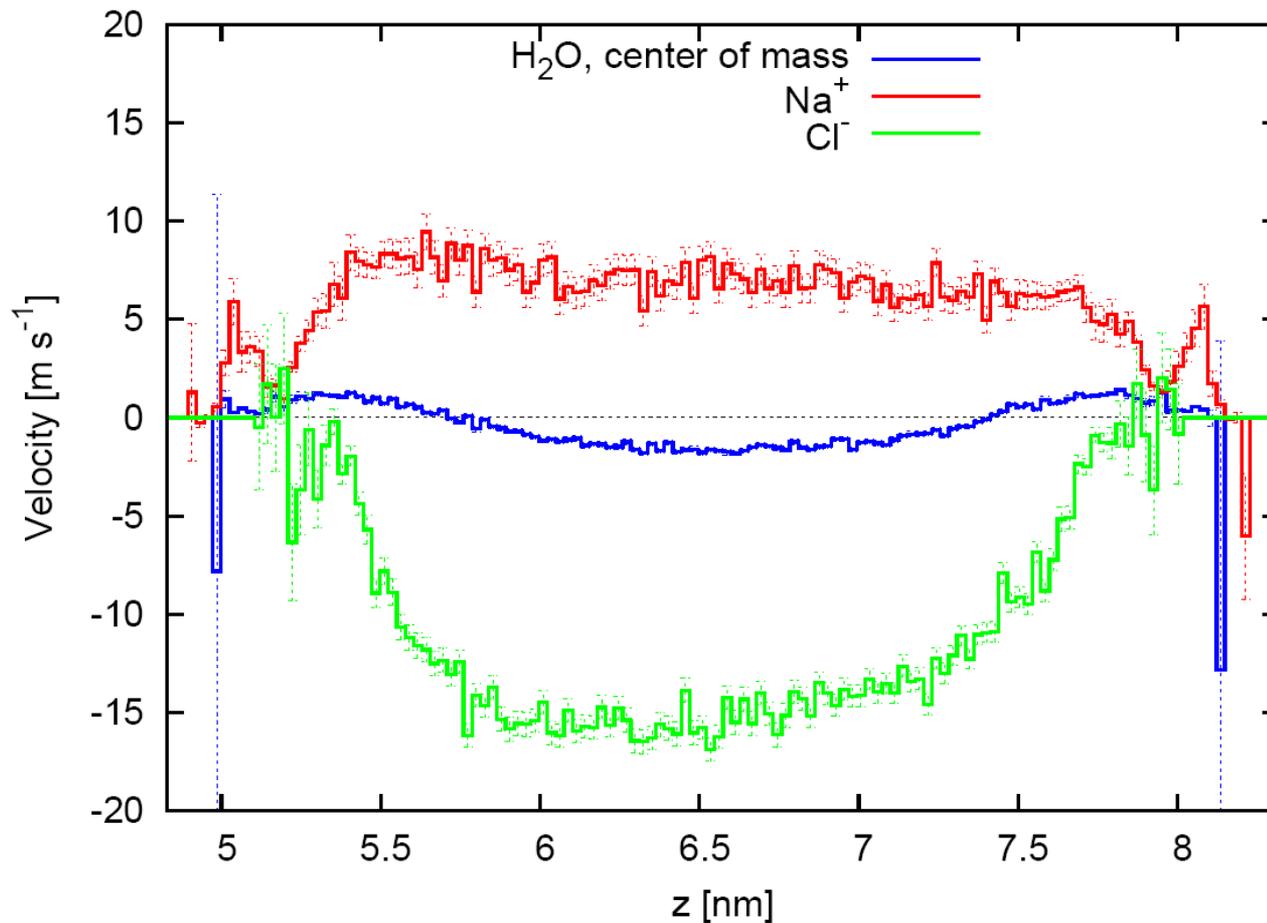
\vec{E}_{ext}

Fixed Si channel walls, innermost layer charged negatively
Dimensions of a solute region 4.66x4.22x3.49 nm, PBC x,y.

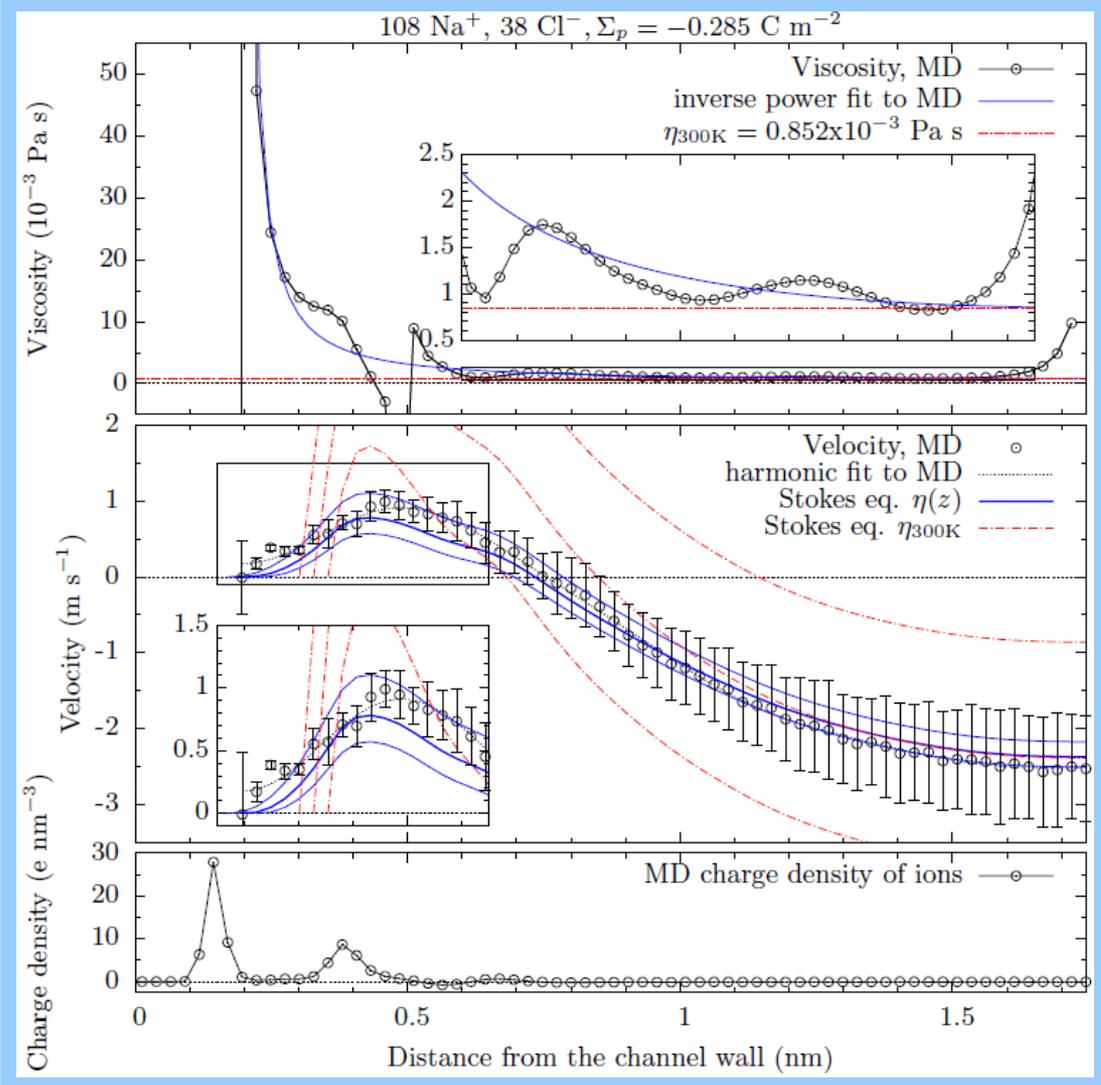
108 Na⁺, 38 Cl⁻, 2144 SPC/E H₂O molecules (not shown)

R. Qiao and N. R. Aluru: Charge Inversion and Flow Reversal in a Nanochannel Electro-osmotic Flow,
PRL 92 (19) 2004

Velocity profiles



Velocity predicted from charge density



Stokes equation:

$$\frac{d}{dz} \left[\eta(z) \frac{du_x(z)}{dz} \right] = -F_d(z)$$

Blue:
inverse power viscosity

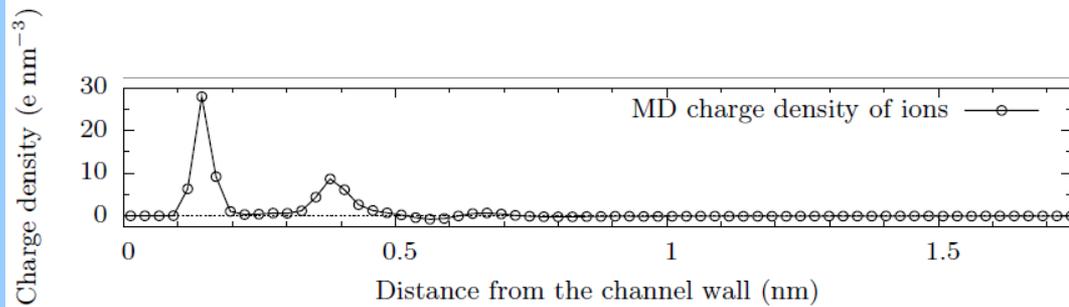
$$\eta(z) = \left[1 - \left(\frac{z}{h} \right)^2 \right]^{-p} \eta_{\text{exp}}$$

Red:
constant viscosity

Black circles:
Molecular Dynamics



Velocity predicted from charge density



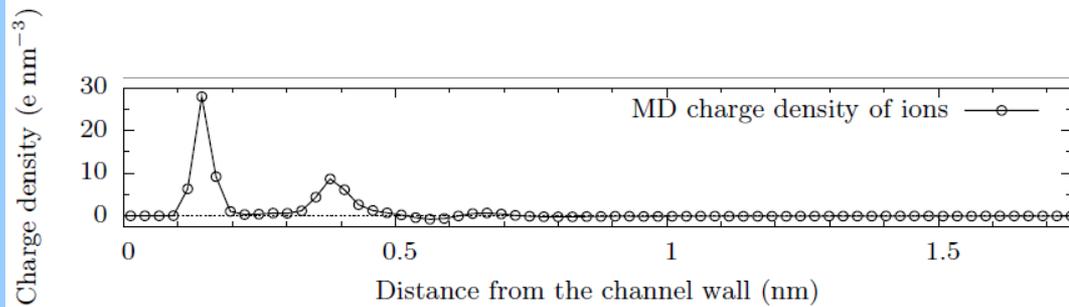
$$\mathbf{F}_d(z) = e [c_{\text{Na}^+}(z) - c_{\text{Cl}^-}(z)] \mathbf{E}_{ext}$$



Velocity predicted from charge density

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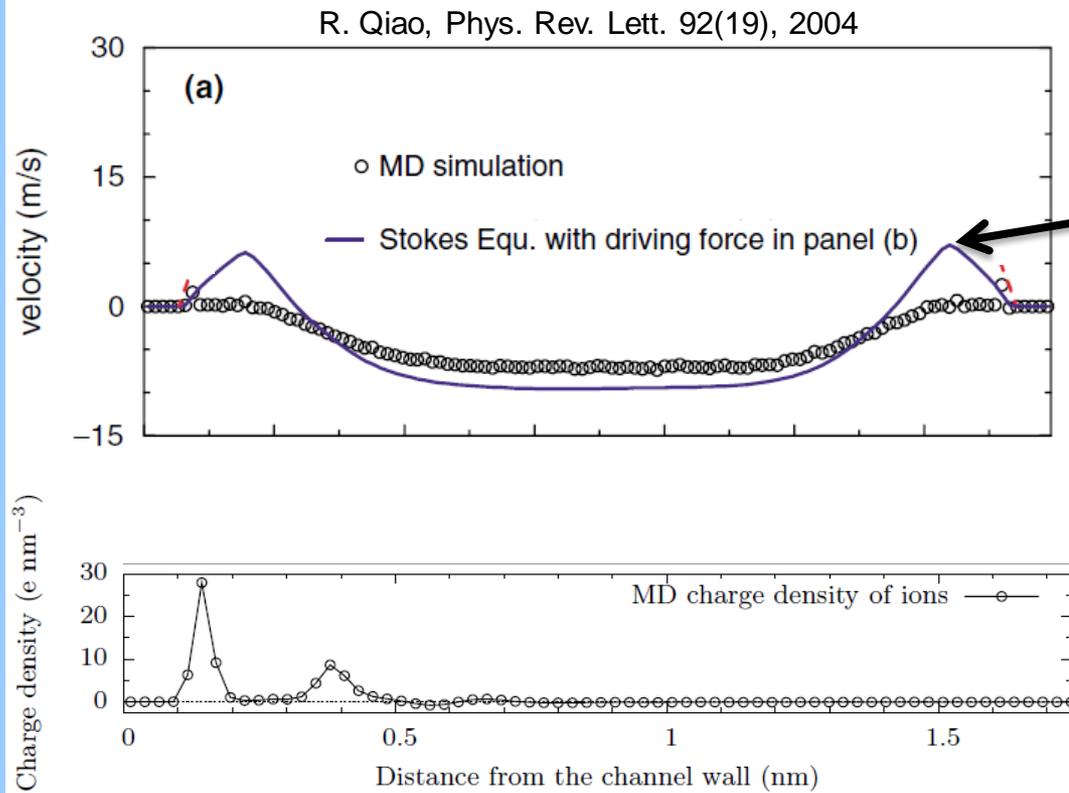
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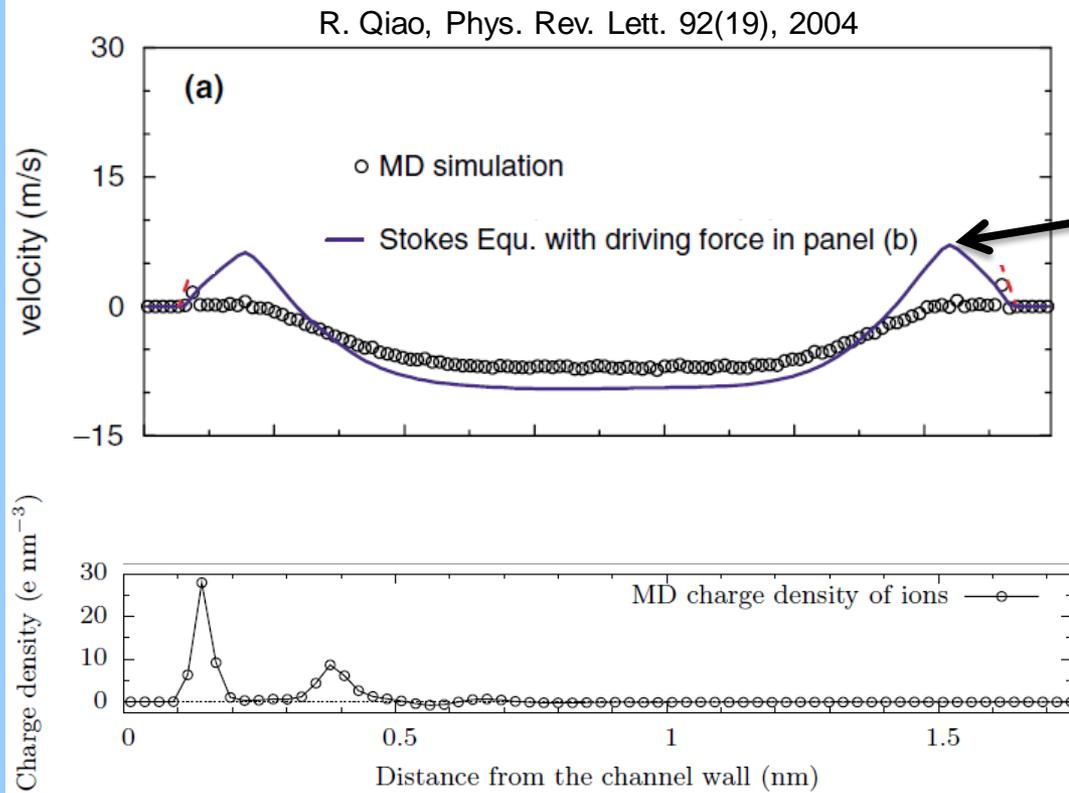
Dark blue line:
velocity prediction
from MD charge density



Velocity predicted from charge density

Stokes equation:

$$\frac{d}{dz} \left[\eta(z) \frac{du_x(z)}{dz} \right] = -F_d(z)$$



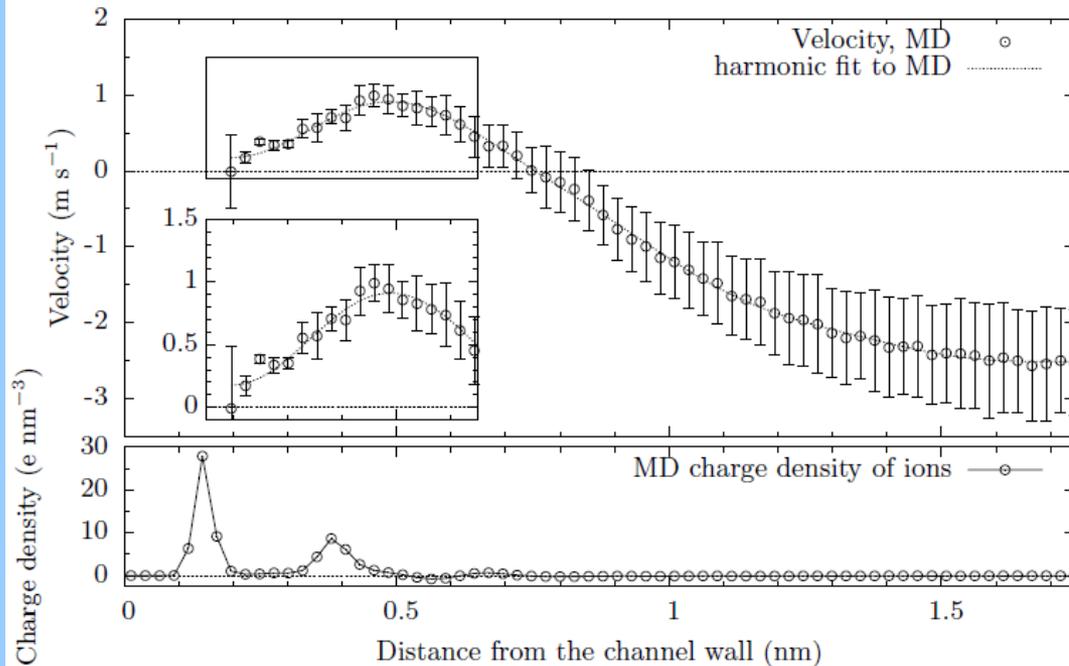
Dark blue line:
velocity prediction
from MD charge density,
assumes constant viscosity



Viscosity estimation

Stokes equation:

$$\frac{d}{dz} \left[\eta(z) \frac{du_x(z)}{dz} \right] = -F_d(z)$$



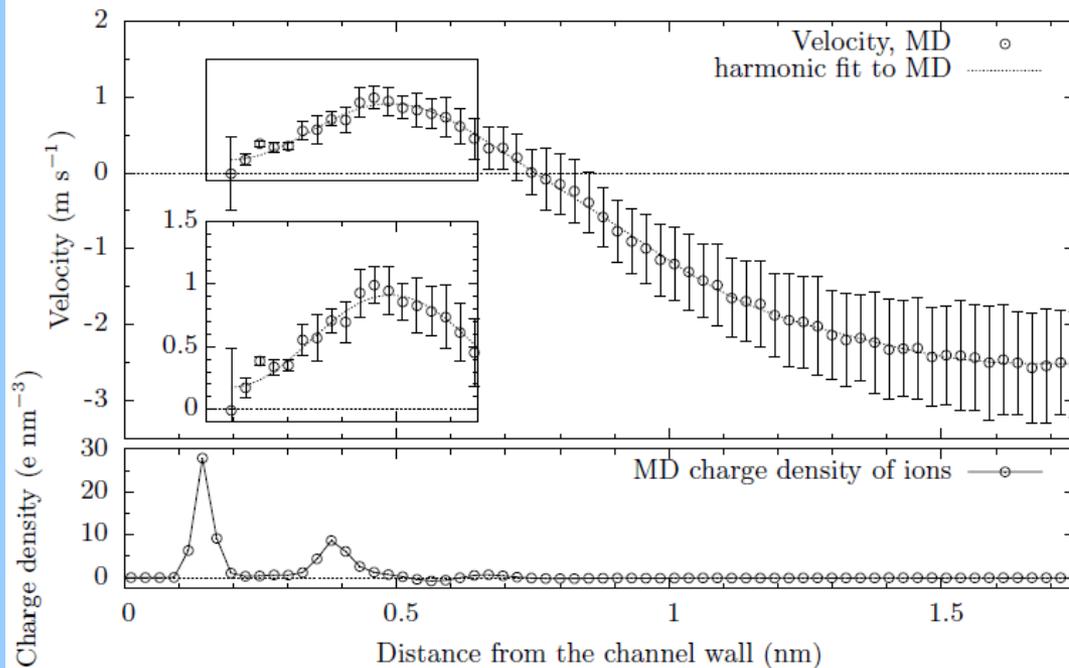
Viscosity estimation

Stokes equation:

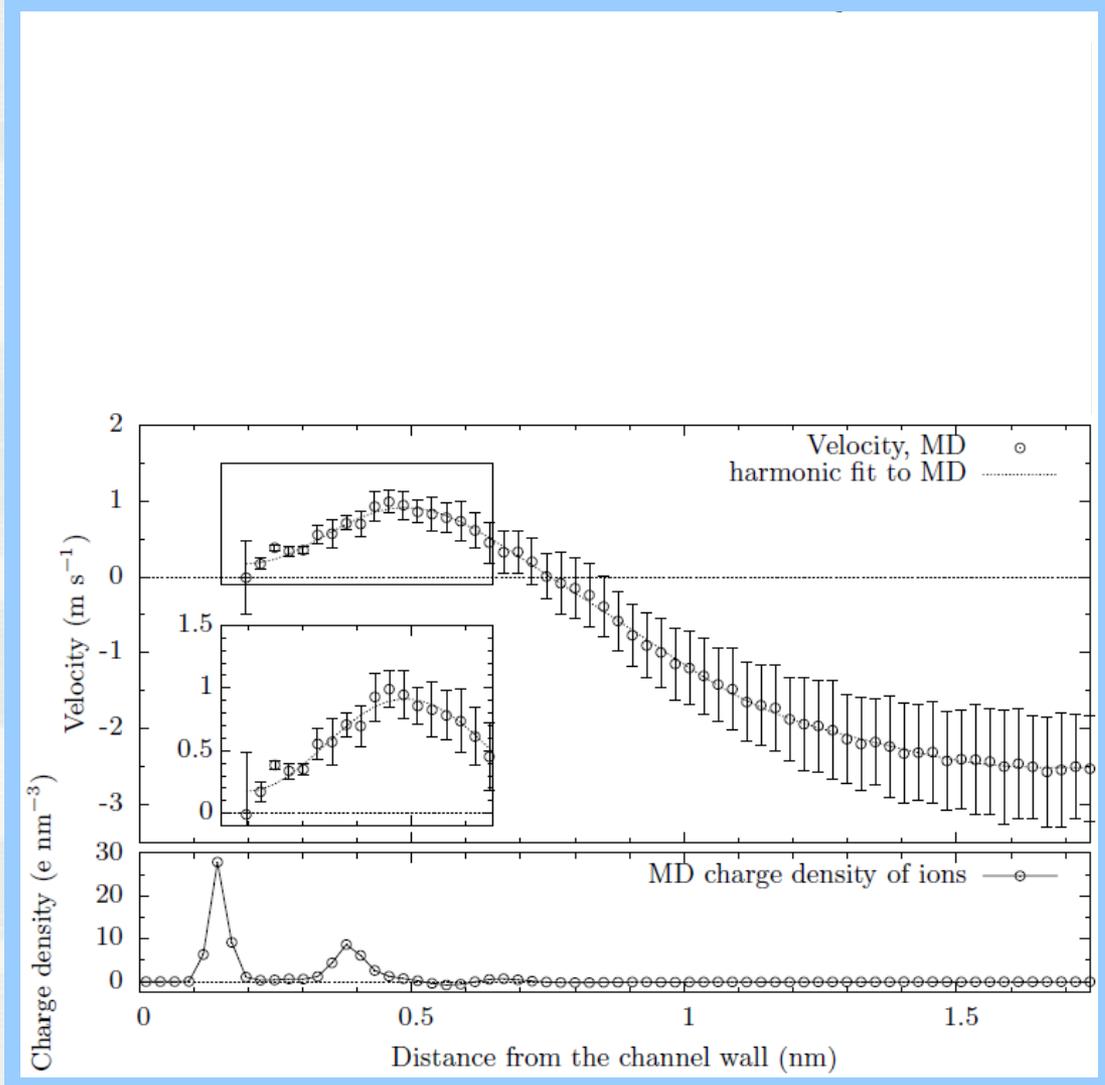
$$\frac{d}{dz} \left[\eta(z) \frac{du_x(z)}{dz} \right] = -F_d(z)$$

Integrated:

$$\eta(z)|_{z=z_0} = \frac{-\int_0^{z_0} F_d(z) dz}{\left. \frac{du_x(z)}{dz} \right|_{z=z_0}}$$



Viscosity estimation



Stokes equation:

$$\frac{d}{dz} \left[\eta(z) \frac{du_x(z)}{dz} \right] = -F_d(z)$$

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Velocity approximation:

$$u_{x fit}(z) = \sum_{n=0}^7 a_n \cos\left(n\pi \frac{z}{h}\right)$$

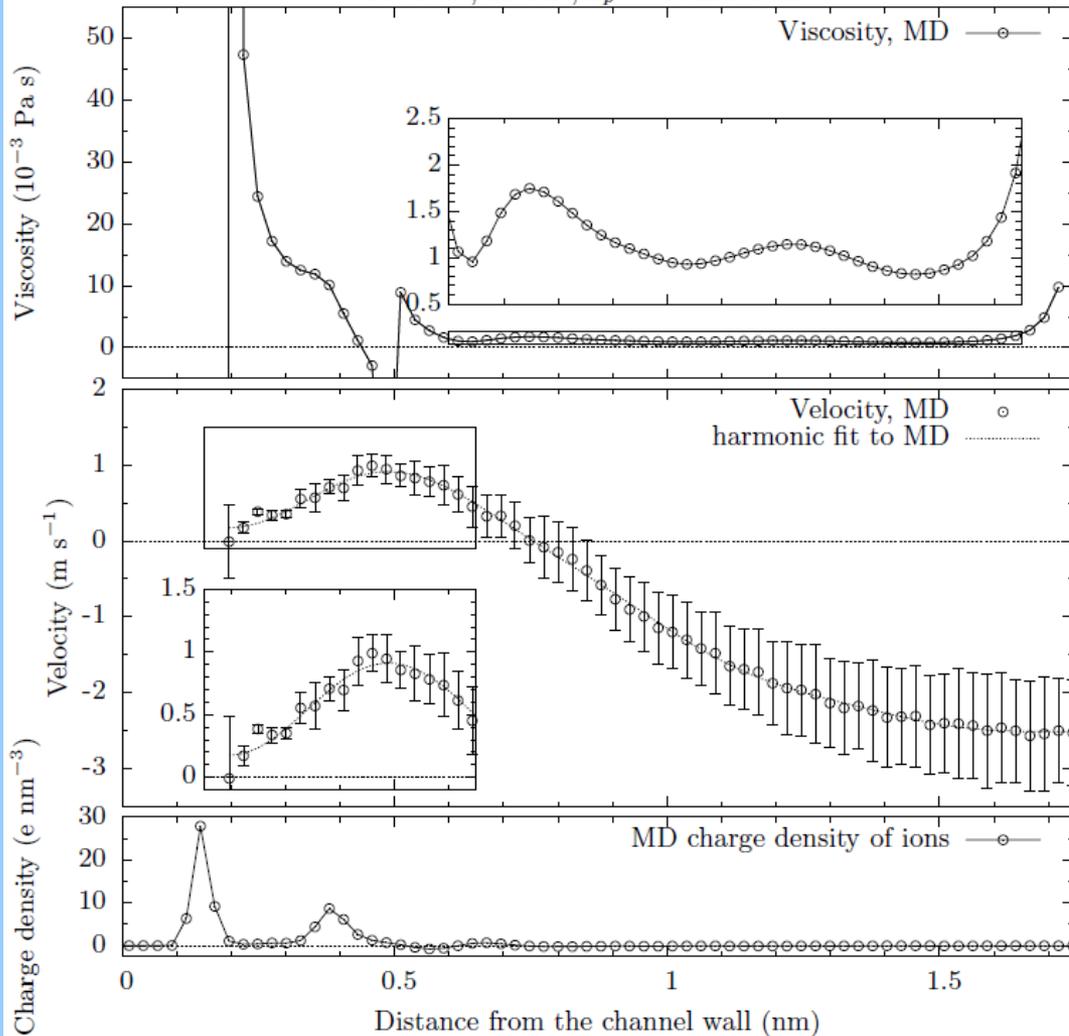
J.B. Freund, J. Chem. Phys. 116(5), 2002

$$u_{fit}(y) = u_m \exp\left[\frac{(y-y_m)^4}{y_1^4}\right] + \sum_{n=0}^{11} a_n \cos\frac{\pi y n}{L}$$



Viscosity estimation

108 Na⁺, 38 Cl⁻, $\Sigma p = -0.285 \text{ C m}^{-2}$



Stokes equation:

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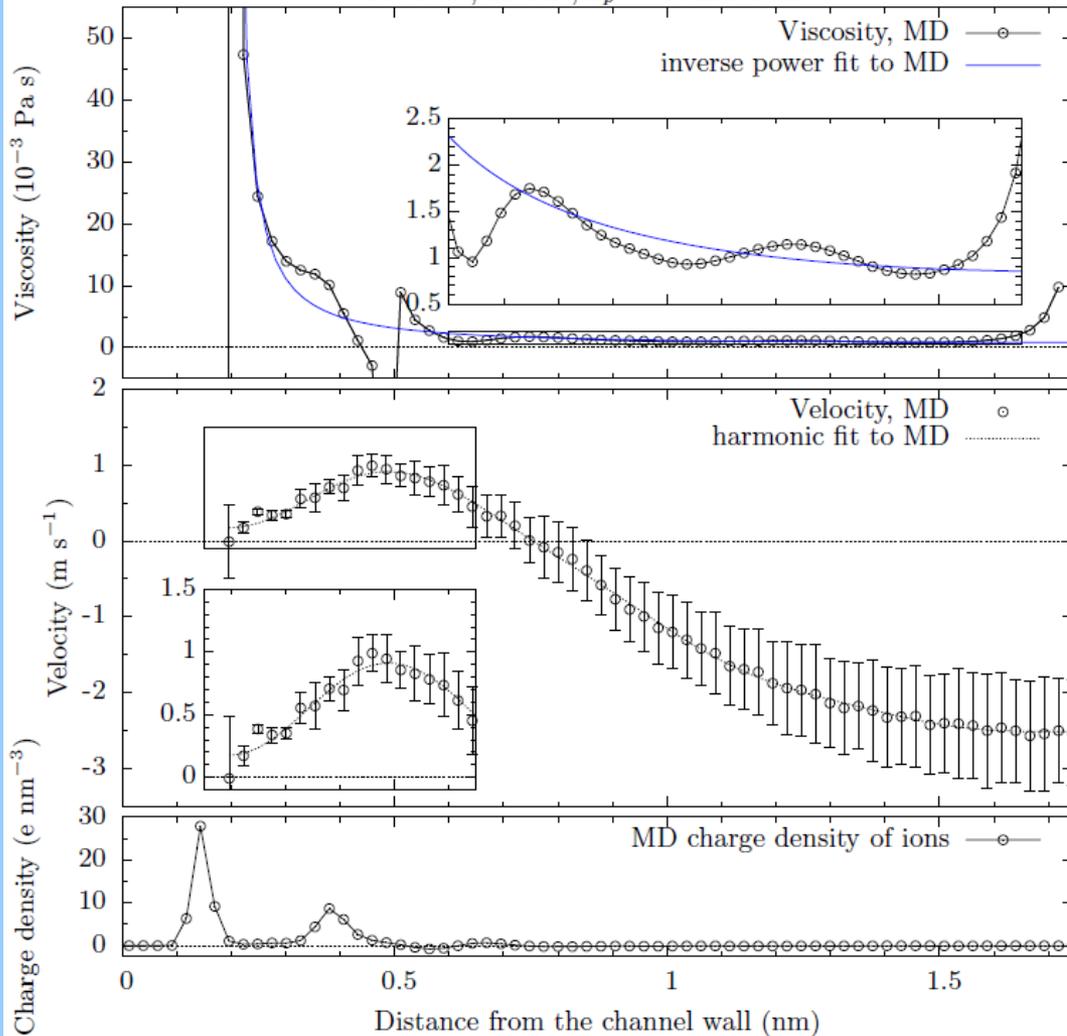
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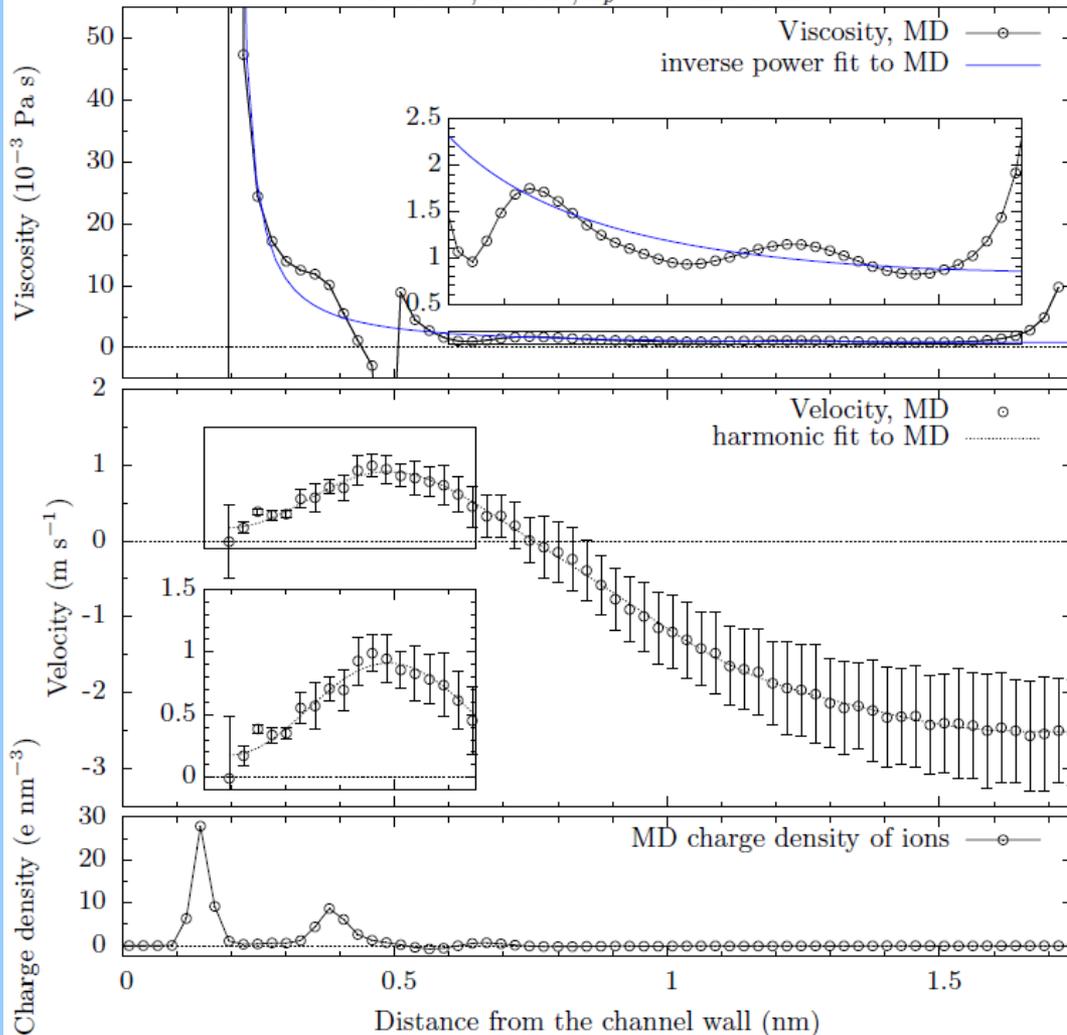
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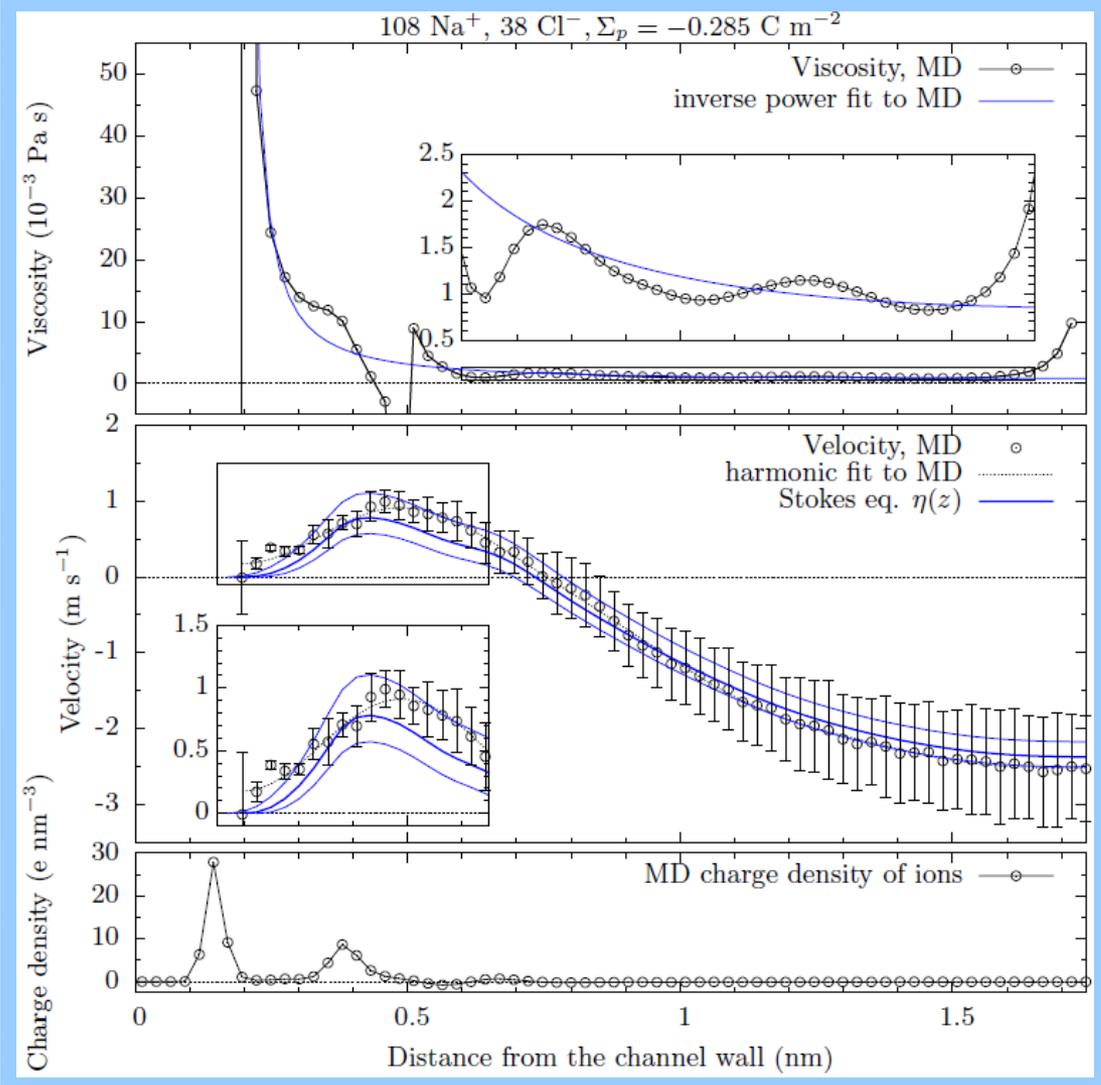
$$\frac{d}{dz} \left[\eta(z) \frac{du_x(z)}{dz} \right] = -F_d(z)$$

Blue:
inverse power viscosity

$$\eta(z) = \left[1 - \left(\frac{z}{h} \right)^2 \right]^{-p} \eta_{\text{exp}}$$



Velocity predicted from charge density



Stokes equation:

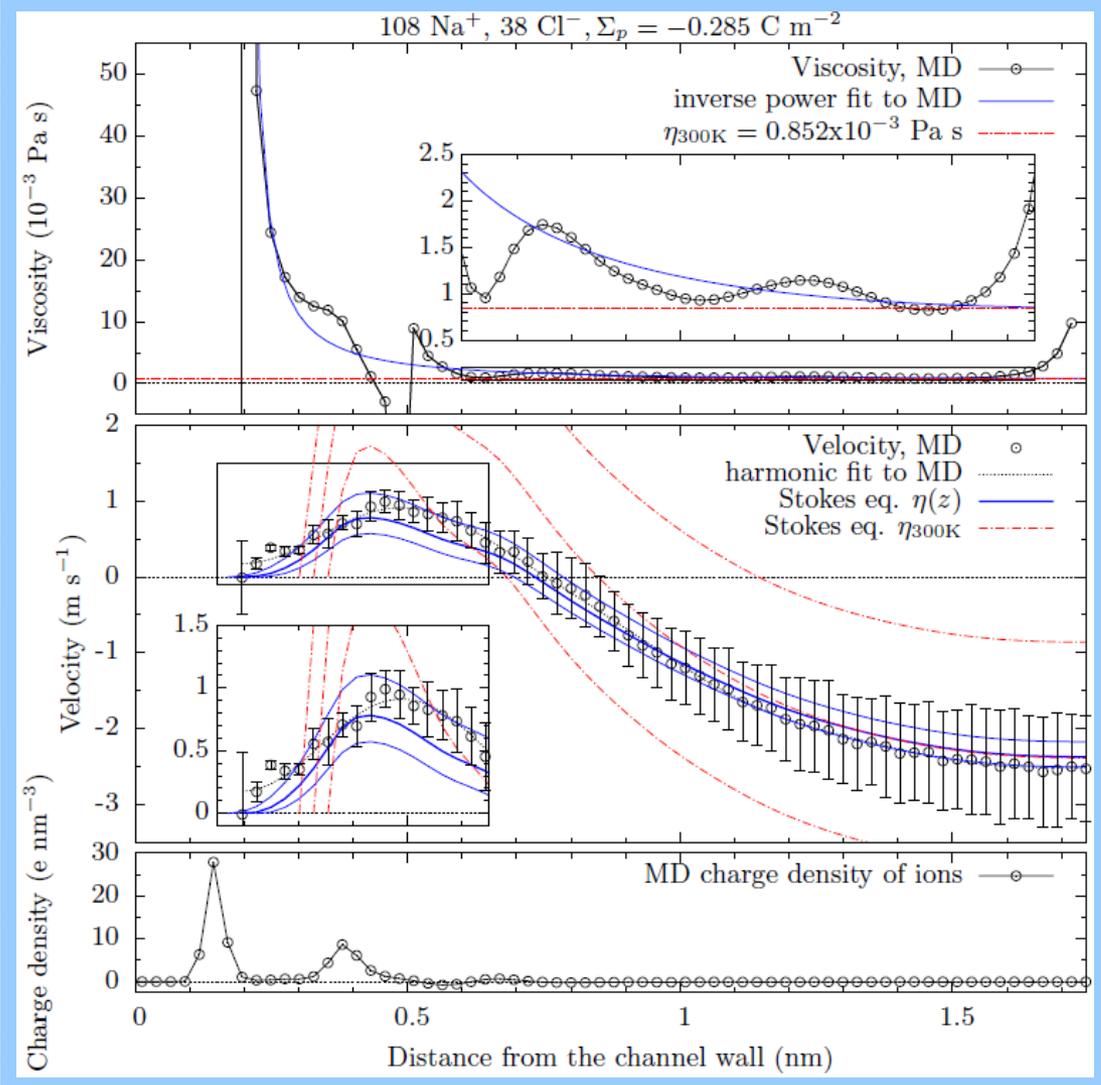
$$\frac{d}{dz} \left[\eta(z) \frac{du_x(z)}{dz} \right] = -F_d(z)$$

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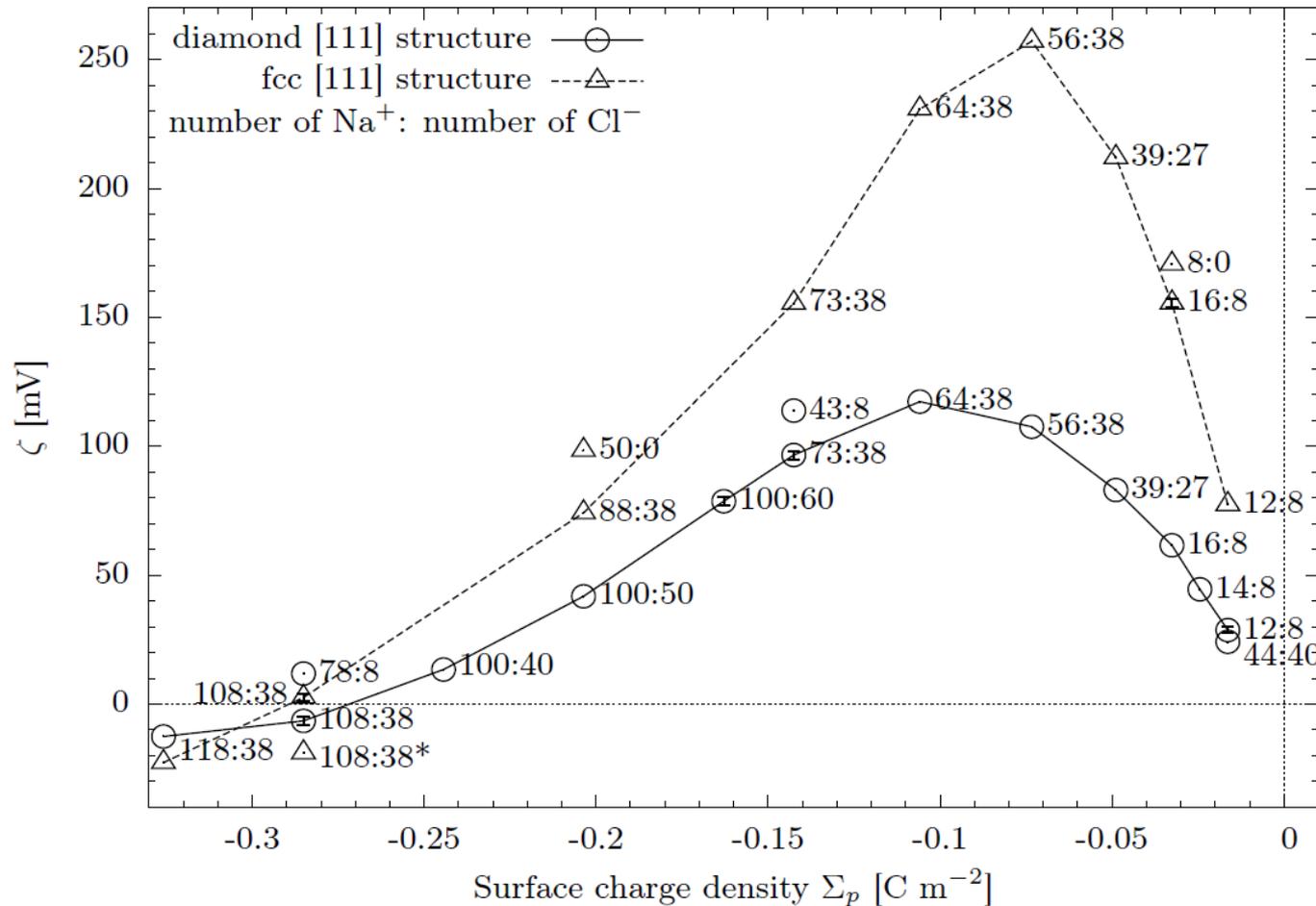
Blue:
inverse power viscosity

$$\eta(z) = \left[1 - \left(\frac{z}{h} \right)^2 \right]^{-p} \eta_{\text{exp}}$$

Red:
constant viscosity



Zeta potentials vs. surf. charge density for uniform partial surface charge



MD Zeta potential:

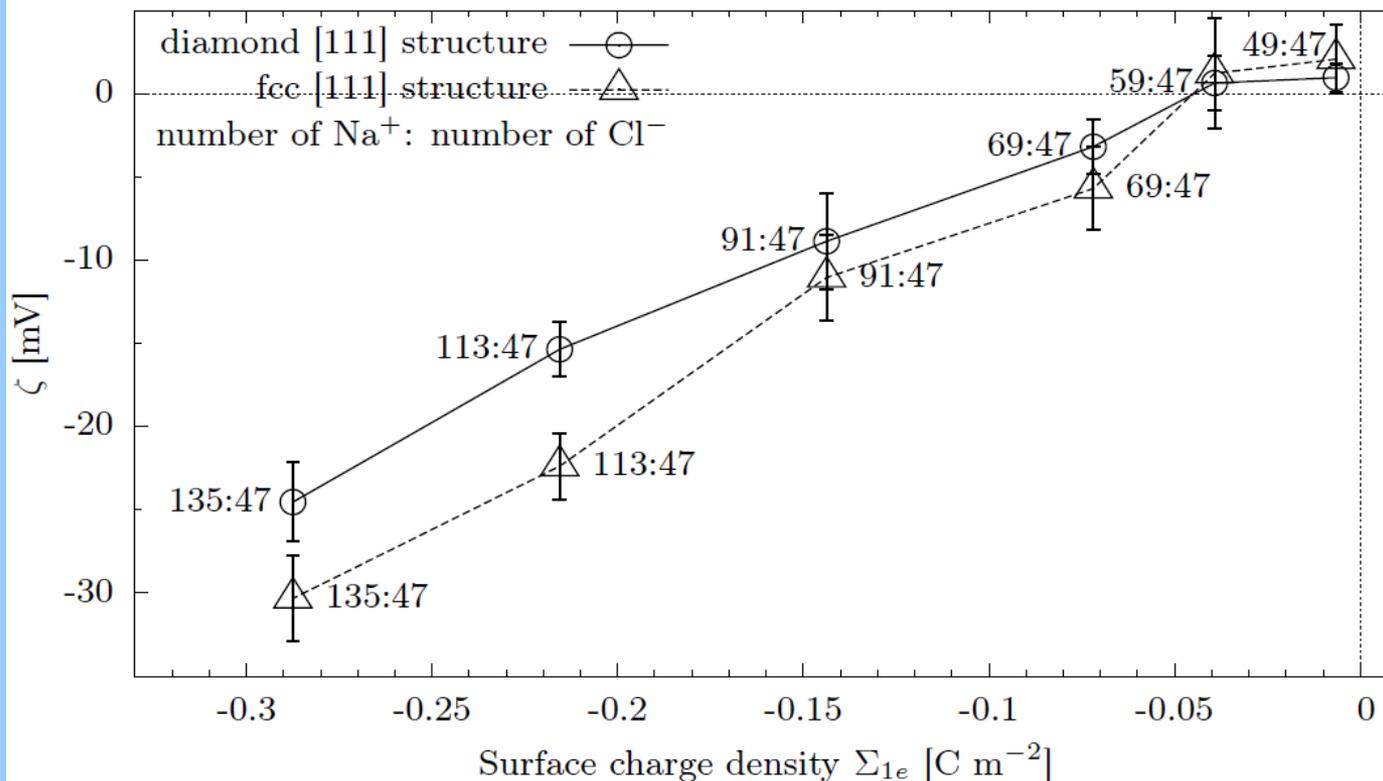
$$\zeta = \frac{u_x(z_{\text{center}})\eta}{\epsilon_0\epsilon_r E_x}$$

Zeta potential is proportional to the water velocity in the channel center.

Assumes u_x is linear in E_x



Zeta potentials vs. surf. charge density for discrete partial surface charge



MD Zeta potential:

$$\zeta = \frac{u_x(z_{\text{center}})\eta}{\epsilon_0\epsilon_r E_x}$$

Zeta potential is proportional to the water velocity in the channel center.

Assumes u_x is linear in E_x



Conclusions

Studied factors significantly affecting nanochannel electro-osmotic flow by MD simulations

Obtained velocity profiles, ionic concentrations, and viscosity profiles

Demonstrated an improved prediction of velocity profile from charge density with non-constant viscosity

Revealed the dependence of the flow on surface charge density, distribution, and ionic concentrations